

NEET PHYSICS NOTES

Motion in a straight line

MOTION IN A STRAIGHT LINE

It deals with the motion of an object which changes its position with time along a straight line.

Kinematics:

The study of the motion of objects without considering the cause of motion is called kinematics.

Rest and Motion:

* **Rest:** If the position of a body does not change with time with respect to the surrounding then it is said to be at rest.

* **Motion:** If the position of a body changes with time with respect to the surrounding then it is said to be in Motion.

Example:

A person standing in a moving bus is at rest with respect to bus and he is in motion with respect to an observer on the ground.

* **Does motion and rest are relative?**

* **Distance:** The actual path covered by a moving particle in a given interval of time.

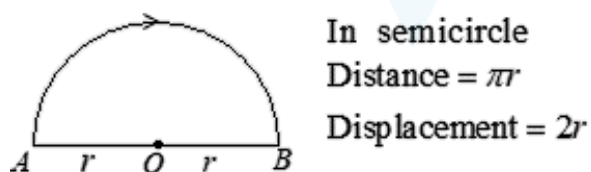
* **Displacement:** The shortest perpendicular distance between initial and final points is called displacement.

$\text{Distance} \geq \text{Displacement}$

* Distance and Displacements both are having same units and dimensional formulas.

$$\text{S.I unit} = m; \quad \text{D.F} = L^1$$

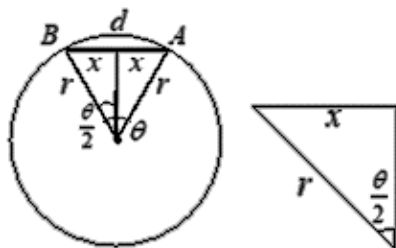
* Distance is a scalar quantity; Displacement is a vector quantity.



If an object turns through an angle θ along a circular path of radius r from point A to point B , then

$$\text{Distance } d = r\theta$$

$$\text{Displacement } 2x = 2r \sin \frac{\theta}{2}$$



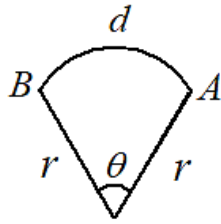
$$\sin\left(\frac{\theta}{2}\right) = \frac{x}{r}$$

$$x = r \sin\left(\frac{\theta}{2}\right)$$

$$\text{Displacement } 2x = 2r \sin\left(\frac{\theta}{2}\right)$$

$$\sin \theta = \frac{\text{length of arc}}{\text{radius}}$$

$$\sin \theta = \frac{AB}{OB} = \frac{d}{r}$$



For smaller angles $\sin \theta \cong \theta$

$$\theta = \frac{d}{r} \Rightarrow d = r\theta$$

$$\text{Displacement } 2x = 2r \sin\left(\frac{\theta}{2}\right)$$

Speed: The rate of change of distances of a moving object is called Speed.

Speed is a scalar

$$\text{S.I unit} = ms^{-1}$$

$$\text{D.F} = LT^{-1}$$

$$\text{Speed} = \frac{\text{distance}}{\text{time}} \Rightarrow v = \frac{s}{t}$$

Velocity: The rate of change of displacement of a moving body is called Velocity.

It is a vector.

$$\text{S.I unit} = ms^{-1}$$

$$\text{D.F} = LT^{-1}$$

$$\text{Velocity} = \frac{\text{displacement}}{\text{time}}$$

$$\vec{v} = \frac{\vec{s}}{t}$$

Average speed: The ratio of total distance travelled by the moving object to time taken.

$$v_{\text{avg}} = \frac{\text{Total distance travelled}}{\text{Total time taken}}$$

$$v_{\text{avg}} = \frac{ds}{dt}$$

Average velocity: The ratio of total displacement to total time taken by a moving object.

$$\vec{v}_{\text{avg}} = \frac{\text{total displacement}}{\text{total time}} = \frac{d\vec{s}}{dt}$$

Instant speed: The speed at a particular instant of time.

$$\text{Instantaneous speed} = \lim_{\Delta t \rightarrow 0} \frac{\Delta s}{\Delta t} = \frac{ds}{dt}$$

Instantaneous velocity: The velocity at a particular instant of time.

$$\text{Instantaneous velocity} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{s}}{\Delta t} = \frac{d\vec{s}}{dt}$$

Uniform motion: If an object moving along a straight line covers equal distances in equal intervals of time is known as uniform motion.

Acceleration:

The rate of change of velocity of a moving body is called acceleration.

Let v_1, v_2 be the velocities of a particle at instances t_1, t_2 respectively then

$$\text{Acceleration} = \frac{\text{change in velocity}}{\text{time}} = \frac{v_2 - v_1}{t_2 - t_1}$$

$$a = \frac{v - u}{t} \text{ (or) } \frac{dv}{dt}$$

S.I unit of $a = ms^{-2}$

D.F for $a = LT^{-2}$

Instantaneous acceleration:

The acceleration at a particular instant of time.

$$\text{Instantaneous acceleration} = \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t} = \frac{dv}{dt}$$

Deceleration [retardation or negative acceleration]:

The velocity of a moving object decreases is called deceleration.

Uniform acceleration:

The velocity either increases or decreases at the same rate throughout the motion.

kinematical equations of motion

$$1. v = u + at$$

$$2. v^2 - u^2 = 2as$$

$$3. s = ut + \frac{1}{2}at^2$$

$$4. s_n = u + a \left[n - \frac{1}{2} \right]$$

s_n = distance travelled in n^{th} second

5. Displacement = (Average velocity) time

$$s = v_{\text{avg}} T = \left(\frac{v + u}{2} \right) T$$

where

u = initial velocity

v = final velocity

s = distance or displacement

a = acceleration

t = time

6. x_i = initial position

x_f = final position then

displacement $s = x_f - x_i$

$$s = ut + \frac{1}{2}at^2$$

$$x_f - x_i = ut + \frac{1}{2}at^2$$

$$x_f = x_i + ut + \frac{1}{2}at^2$$

General method:

Acceleration = $\frac{\text{change in velocity}}{\text{time}}$

$$a = \frac{v - u}{t}$$

$$at = v - u$$

$$v = u + at$$

$$v_{\text{avg}} = \frac{s}{t}$$

$$v_{\text{avg}} = \frac{v + u}{2}$$

$$\frac{s}{t} = \frac{v + u}{2}$$

$$\frac{s}{t} = \frac{u + at + u}{2}$$

$$\frac{s}{t} = \frac{2u + at}{2}$$

$$\frac{s}{t} = \frac{2u}{2} + \frac{at}{2}$$

$$s = ut + \frac{1}{2}at^2 \rightarrow (2)$$

$$v = u + at$$

$$v - u = at \rightarrow (a)$$

$$\frac{s}{t} = \frac{v + u}{2}$$

$$v + u = \frac{2s}{t} \rightarrow (b)$$

$a \times b$:

$$(v+u)(v-u) = \frac{2s}{t} \times at$$

$$v^2 - u^2 = 2as \rightarrow (3)$$

Acceleration due to gravity g :

The uniform acceleration of a freely falling body towards the centre of the earth due to earth's gravitational force. It is represented by g .

Its value is constant for all bodies at a given place.

$$g = 9.8 \text{ ms}^{-2} \rightarrow \text{SI}$$

$$g = 980 \text{ cm}^{-2} \rightarrow \text{C.G.S.}$$

→ When a body is falls freely velocity is increases.

g is +ve sign.

→ When a body is projected vertically upwards velocity is decreases.

g is -ve sign.

→ The acceleration due to gravity at the centre of the earth is zero

Equations of motion for a freely falling body:

$$1. \ v = u + at$$

$$v = 0 + gt$$

$$v = gt$$

$$2. \ v^2 - u^2 = 2as$$

$$v^2 - 0 = 2(g)s$$

$$v^2 = 2gs$$

$$v = \sqrt{2gs}$$

$$3. \ s = ut + \frac{1}{2}at^2$$

$$s = (0)t + \frac{1}{2}gt^2$$

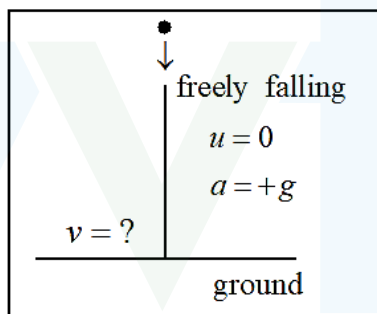
$$s = \frac{1}{2}gt^2$$

$$2s = gt^2$$

$$t = \sqrt{\frac{2s}{g}}$$

If $s = h$

$$\text{Then } t = \sqrt{\frac{2h}{g}}$$



$$4. s_n = u + a \left[n - \frac{1}{2} \right]$$

$$s_n = 0 + g \left[n - \frac{1}{2} \right]$$

$$s_n = g \left[n - \frac{1}{2} \right]$$

Equation of motion for vertically projected body upwards:

$$1. v = u + at$$

$$v = u - gt$$

$$2. v^2 - u^2 = 2as$$

$$v^2 - u^2 = 2(-g)s$$

$$v^2 - u^2 = -2gs$$

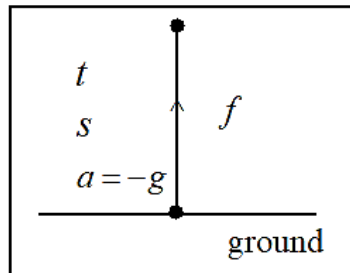
$$v^2 = u^2 - 2gs$$

$$v = \sqrt{u^2 - 2gs}$$

$$ut + \frac{1}{2}at^2$$

$$4. s_n = u + a \left[n - \frac{1}{2} \right]$$

$$s_n = u - g \left[n - \frac{1}{2} \right]$$



Motion parameters of a body projected vertically upwards:

Maximum Height:

For a body projected vertically upwards the maximum vertical displacement with which its final velocity becomes zero called maximum height.

Proof:-

Consider a body is projected vertically upwards with an initial velocity is ' u '?

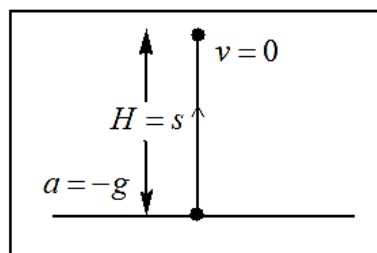
$$\rightarrow \text{from } v^2 - u^2 = 2as$$

$$0^2 - u^2 = 2(-g)H$$

$$-u^2 = -2gH$$

$$u^2 = 2gH$$

$$H = \frac{u^2}{2g}$$



Time of ascent:

The time taken by a vertically projected body to reach its maximum height is called Time of ascent.

Proof:-

$$t = t_a \quad v = u + at$$

$$v = 0 \quad 0 = u + (-g)t_a$$

$$u = u \quad 0 = u - gt_a$$

$$a = -g \quad gt_a = u$$

$$t_a = \frac{u}{g}$$

Time of descent:

For a body projected upwards, the time taken from maximum height to reach the ground [point of projection] is called time of descent.

$$s = ut + \frac{1}{2}at^2$$

$$H = (0)t + \frac{1}{2}(g)t^2$$

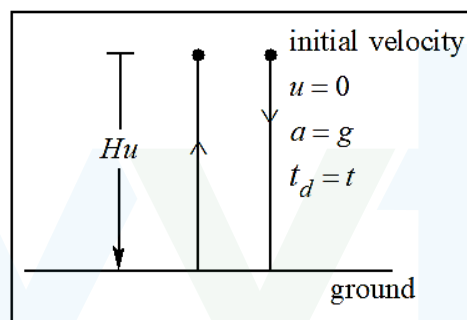
$$H = \frac{gt^2}{2}$$

$$\frac{u^2}{2g} = \frac{gt^2}{2}$$

$$t^2 = \frac{u^2}{g^2}$$

$$t = \frac{u}{g}$$

$$t_d = \frac{u}{g}$$

**Time of flight:**

For a body projected vertically upwards sum of time of descent and the time of ascent is called time of flight.

$$t_f = t_a + t_d = \frac{u}{g} + \frac{u}{g}$$

$$t_f = \frac{2u}{g}$$

Velocity of the body on reaching the point of projection $\left[v_{\text{striking}} \right]$

Consider a body is projected vertically upwards with an initial velocity u . The body reaches the point of projection once again after a time of flight (t_f)

We know that

$$v = u + at$$

$$v = v, a = -g$$

$$t = t_f = \frac{2u}{g}$$

$$v_{\text{striking}} = u - g[t_f]$$

$$v_{\text{striking}} = u - \frac{2ug}{g} = u - 2u$$

$$v_{\text{striking}} = -u \rightarrow (1)$$

upwards

$$v^2 - u^2 = 2as$$

$$0^2 - u^2 = 2(-g)H$$

$$-u^2 = -2gh$$

$$u^2 = 2gh$$

$$u = \sqrt{2gh} \rightarrow (2)$$

From eqn. (1) and (2)

$$v_{\text{striking}} = -u = -\sqrt{2gH}$$

The body reaches the point of projection with the same speed of projection but in opposite direction.

Vertical projection of an object from a tower

[Equation for height of the tower]

Body is projected upwards

$$\text{Total displacement } s = x - x - H = -H$$

$$\text{Time} = t$$

$$\text{Initial velocity} = u$$

$$a = -g$$

$$\text{From } s = ut + \frac{1}{2}at^2$$

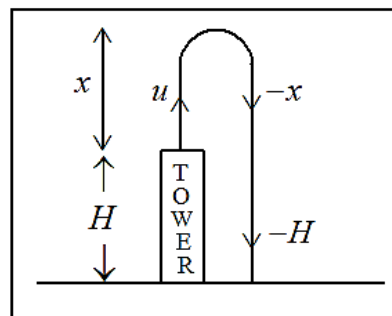
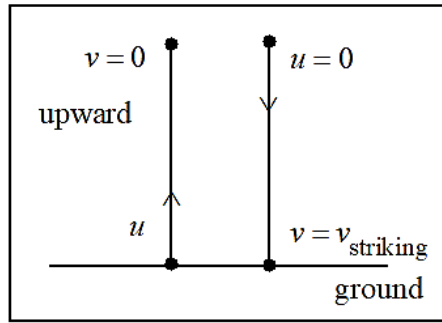
$$-H = ut + \frac{1}{2}(-g)t^2$$

$$-H = ut - \frac{1}{2}gt^2$$

$$H = -ut + \frac{1}{2}gt^2$$

$$\frac{1}{2}gt^2 - ut - H = 0$$

$$ax^2 + bx + c = 0$$



quadratic expression

$$t = \frac{u \pm \sqrt{u^2 + 2gH}}{g}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Consider a tower of height. Let a body is projected upwards vertically with initial velocity u from the top of tower as shown in the above picture.

→ A body dropped freely from a multistored building can reach the ground in t_1 sec. It is stopped in its path after t_2 sec. and again dropped freely from the point. Find the further time taken by it to reach the ground.

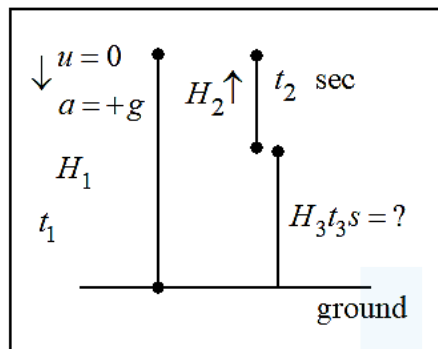
$$s = ut + \frac{1}{2}at^2$$

$$H_1 = (0)t_1 + \frac{1}{2}gt_1^2$$

$$H_1 = \frac{1}{2}gt_1^2$$

$$H_2 = \frac{1}{2}gt_2^2$$

$$H_3 = \frac{1}{2}gt_3^2$$



From the figure

$$H_1 = H_2 + H_3$$

$$\frac{1}{2}gt_1^2 = \frac{1}{2}gt_2^2 + \frac{1}{2}gt_3^2$$

$$t_1^2 = t_2^2 + t_3^2$$

$$t_3^2 = t_1^2 - t_2^2$$

$$t_3 = \sqrt{t_1^2 - t_2^2}$$

→ Body I is released from top of tower at the same time is projected vertically upwards as shown in the figure.

Let the two meet after a time t seconds

$$t_1 = t_2 = t \text{ sec} = ?$$

Body I

Body II

$$u = 0, a = +g \quad s = ut + \frac{1}{2}at^2$$

$$s = ut + \frac{1}{2}at^2 \quad s_2 = ut + \frac{1}{2}(-g)t^2$$

$$s_1 = (0)t + \frac{1}{2}gt^2 \quad s_1 = ut - \frac{1}{2}gt^2$$

$$s_1 = \frac{1}{2}gt^2$$

We know that

$$h = s_1 + s_2 = \frac{1}{2}gt^2 + ut - \frac{1}{2}gt^2$$

$$h = ut$$

$$t = \frac{h}{u}$$

→ At what time their velocity are equal for body I freely falling $u = 0, a = +g, t = t$

$$v = u + at$$

$$v = 0 + gt$$

$$v_1 = gt$$

For body II

$$u = u \quad a = -g$$

$$t = t \quad v = v_2$$

From $v = u + at$

$$v_2 = u - gt$$

Given $v_1 = v_2$

$$gt = u - gt$$

$$gt + gt = u$$

$$2gt = u$$

$$t = \frac{u}{2g}$$

→ Find their ratio of distance covered their velocities are equal at $t = \frac{u}{2g}$

$$s_1 = \frac{1}{2}gt^2 = \frac{g}{2} \left[\frac{u}{2g} \right]^2 = \frac{g}{2} \left[\frac{u^2}{4g^2} \right] = \frac{u^2}{8g}$$

$$s_2 = ut - \frac{1}{2}gt^2 = u \cdot \left[\frac{u}{2g} \right] - \frac{u^2}{8g} = \frac{u^2}{2g} - \frac{u^2}{8g}$$

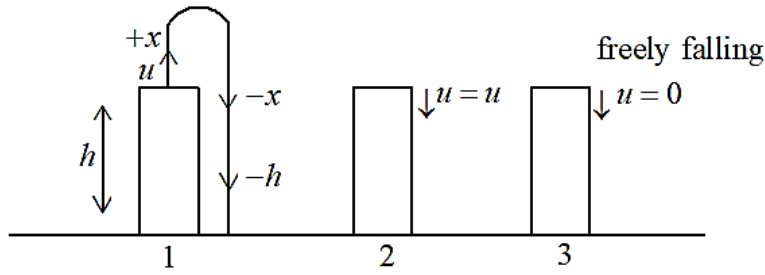
$$s_2 = \frac{4u^2 - u^2}{8g} = \frac{3u^2}{8g}$$

$$\frac{s_1}{s_2} = \frac{\frac{u^2}{8g}}{\frac{3u^2}{8g}} = \frac{1}{3}$$

$$s_1 : s_2 = 1 : 3$$

→ Three bodies are projected from towers of same height as shown. 1st one is projected vertically upwards with velocity u the 2nd one is thrown down vertically with the same velocity and the 3rd one is dropped as freely falling body.

If t_1, t_2, t_3 are the times taken by them to reach the ground, then



For 1st body, $h = -ut_1 + \frac{1}{2}gt_1^2 \rightarrow (1)$

vertically upwards

2nd body, $h = ut_2 + \frac{1}{2}gt_2^2 \rightarrow (2)$

3rd body, $h = \frac{1}{2}gt_3^2 \rightarrow (3)$

eq. (1) $\times t_2 \rightarrow ht_2 = -ut_1t_2 + \frac{1}{2}gt_1^2t_2$

eq. (2) $\times t_1 \rightarrow ht_1 = ut_2t_1 + \frac{1}{2}gt_2^2t_1$

$$h(t_2 + t_1) = \frac{g}{2} \left[t_1t_2 + \frac{gt_1t_2}{2} [t_1 + t_2] \right]$$

$h = \frac{gt_1t_2}{2} \rightarrow (4)$

From eqns. (3) and (4)

$$\frac{1}{2}gt_3^2 = \frac{gt_1t_2}{2}$$

$$t_3^2 = t_1t_2$$

$$t_3 = \sqrt{t_1t_2}$$

$\rightarrow \text{eq. (1)} = \text{eq. (2)}$

$$-ut_1 + \frac{1}{2}gt_1^2 = ut_2 + \frac{1}{2}gt_2^2$$

$$\frac{1}{2}g[t_1^2 - t_2^2] = ut_2 + ut_1$$

$$\frac{g}{2}[t_1^2 - t_2^2] = u[t_1 + t_2]$$

$$\frac{g}{2}[t_2 - t_1][t_2 + t_1] = u[t_1 + t_2]$$

Velocity of projection $u = \frac{g}{2}(t_2 - t_1) \rightarrow \text{eq. (6)}$

Time difference b/w first two bodies to reach the ground, $\Delta t = \frac{2u}{g}$

From eq. (6)

$$2u = g(t_2 - t_1)$$

$$\frac{2u}{g} = t_2 - t_1 = \Delta t$$

For a freely falling body the ratio of distances travelled in 1 second, 2 seconds, 3 seconds is

In case of freely falling

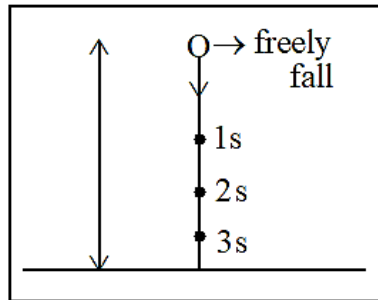
$$u = 0, a = g, t = t$$

$$\text{From } s = ut + \frac{1}{2}at^2$$

$$s = (0)t + \frac{1}{2}gt^2$$

$$s = \frac{1}{2}gt^2$$

$$s \propto t^2$$



$$\text{If } t = 1 \text{ sec then } s_1 = \frac{1}{2}g(1)^2 = \frac{g}{2}[1]$$

$$\text{If } t = 2 \text{ sec then } s_2 = \frac{1}{2}g(2)^2 = \frac{g}{2}[4]$$

$$\text{If } t = 3 \text{ sec then } s_3 = \frac{1}{2}g(3)^2 = \frac{g}{2}[9]$$

$$\text{If } t = 4 \text{ sec then } s_4 = \frac{1}{2}g(4)^2 = \frac{g}{2}[16]$$

$$\therefore s_1 : s_2 : s_3 : s_4 : \dots = 1 : 4 : 9 : 16 : \dots$$

For a freely falling body the ratio of distances travelled in 1st, 2nd, 3rd sec..... is

In case of freely falling

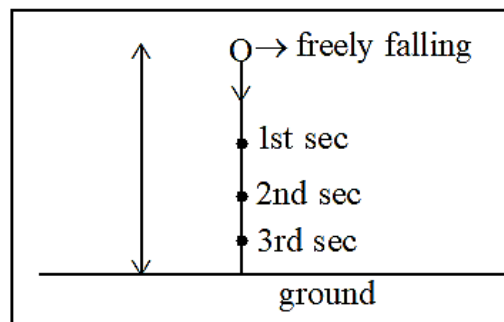
$$u = 0, a = g, t = t$$

$$\text{From } s_n = u + a \left[1 - \frac{n}{2} \right]$$

$$s_n = 0 + g \left[n - \frac{1}{2} \right]$$

$$s_n = \frac{g}{2}[2n - 1]$$

$$s_n \propto (2n - 1)$$



$$\text{If } n = 1^{\text{st}} \text{ sec then } s_1 = \frac{g}{2}[2 - 1] = \frac{g}{2}$$

$$\text{If } t = 2^{\text{nd}} \text{ sec then } s_2 = \frac{g}{2}[4 - 1] = \frac{3g}{2}$$

If $t = 3^{\text{rd}}$ sec then $s_3 = \frac{g}{2}[6-1] = \frac{5g}{2}$

If $t = 4^{\text{th}}$ sec then $s_4 = \frac{g}{2}[8-1] = \frac{7g}{2}$

If $t = 5^{\text{th}}$ sec then $s_5 = \frac{g}{2}[10-1] = \frac{9g}{2}$

$$s_1 : s_2 : s_3 : s_4 : s_5 : \dots = 1 : 3 : 5 : 7 : 9 : \dots$$

A stone is dropped into a well of depth ' h ' then the sound of splash is heard after a time t is

Free falling

$$u = 0, a = +g, s = h$$

$$s = ut_1 + \frac{1}{2}at_1^2$$

$$h = (0)t_1 + \frac{1}{2}gt_1^2$$

$$\frac{gt_1^2}{2} = h$$

$$t_1 = \sqrt{\frac{2h}{g}}$$

time taken by the body to touches the water.

Time taken by the sound to travel a distance of h ,

$$\text{Velocity} = \frac{\text{displacement}}{\text{time}}$$

$$v_{\text{sound}} = \frac{h}{t_2}$$

$$t_2 = \frac{h}{v_{\text{sound}}}$$

Time to hear splash of sound is

$$t = t_1 + t_2 = \sqrt{\frac{2h}{g}} + \frac{h}{v_{\text{sound}}}$$

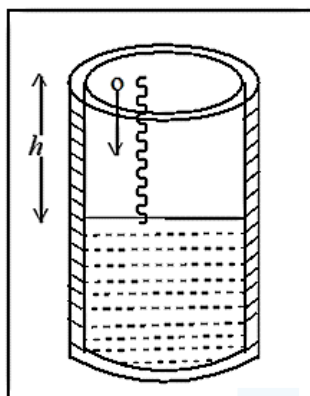
If a particle starts from rest and moves with uniform acceleration a such that it travels a distances S_m and

S_n in m^{th} and n^{th} seconds then

$$s_n = u + a \left[n - \frac{1}{2} \right]$$

$$s_m = u + a \left[n - \frac{1}{2} \right]$$

Rest $u = 0$



$$s_n = 0 + a \left[n - \frac{1}{2} \right]$$

$$s_n = a \left(\frac{2n-1}{2} \right)$$

$$s_m = a \left[\frac{2m-1}{2} \right]$$

$$s_n - s_m = \frac{a}{2} [2n-1-2m+1]$$

$$s_n - s_m = \frac{a}{2} [2n-2m]$$

$$s_n - s_m = a[n-m]$$

$$a = \frac{s_n - s_m}{n - m}$$

If a particle starts from rest and moves with uniform acceleration 'a'

If s is the distance travelled in n seconds

$$t = n \text{ sec}$$

$$\text{rest } u = 0$$

$$s = ut + \frac{1}{2} at^2$$

$$s = 0(n) + \frac{1}{2} an^2$$

$$s = \frac{an^2}{2} \rightarrow (1)$$

If s_n is the distance travelled in n^{th} second

$$s_n = u + a \left[\frac{2n-1}{2} \right]$$

$$s_n = 0 + a \left(\frac{2n-1}{2} \right)$$

$$s_n = \frac{a}{2} (2n-1) - 2$$

$$\frac{s_n}{s} = \frac{\frac{a}{2} (2n-1)}{\frac{a}{2} (n^2)}$$

$$\frac{s_n}{s} = \frac{2n-1}{n^2}$$

→ A stone is dropped into a river from the bridge and after a time x sec another stone is projected down into the river from the same point with a velocity 'u'

If both stones reaches the water simultaneously then

1st stone freely falling

$$u = 0$$

$$a = +g$$

$$t_1 = t \text{ second}$$

$$s = ut + \frac{1}{2}at^2$$

$$s_1 = (0)t + \frac{1}{2}gt^2$$

$$s_1 = \frac{1}{2}gt^2$$

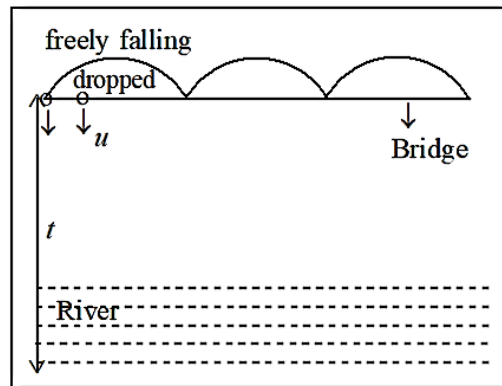
2nd stone thrown downwards

$$u = u$$

$$a = +g$$

$$t_2 = t - x$$

$$s_2 = u(t - x) + \frac{1}{2}g(t - x)^2$$



Motion Curves:-

Graphical analysis is a convenient method of studying the motion of a particle. It can be effectively applied to analyse the motion of situation of a particle. For graphical representation we required two coordinate axes.

One is independent variable along x-axis and the dependent variable along y-axis

Ex:- With time as one of the variable it usually taken along x-axis (since it is independent) and the other variable is along y-axis.

In many problems either slope or area both has to be determined to explained or understand the motion of a particle.

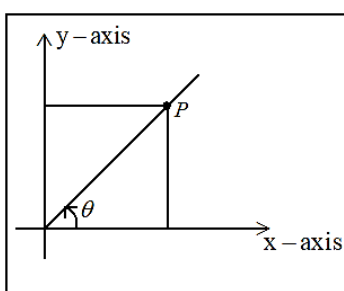
Slope of a straight line is determined by two methods

In the first method:

The St. line whose slope has to be determined is extended the angle made by the line with x-axis is noted the tangent to that angle gives slope of the straight line.

If ' θ ' is the angle made by extended line with x-axis as shown in the figure.

$$\text{Slope}(m) = \tan \theta$$

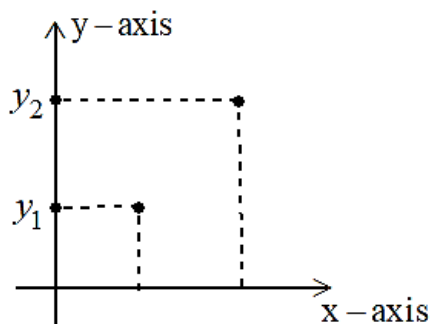


2nd method:

Any two points on the line ⊥ lers are drawn on to both x and y axes. Their respective coordinates (foot of ⊥ lers) are noted. The ratio of difference of y-coordinates to x-coordinates gives the slope of this straight line.

Let A and B are two points on the St. line

The slope of St. line $m = \frac{y_2 - y_1}{x_2 - x_1}$



Position - time graph's [x-t graph]:

Graphs are drawn with time along x axis and position [displacement w.r.t origin] along y axis

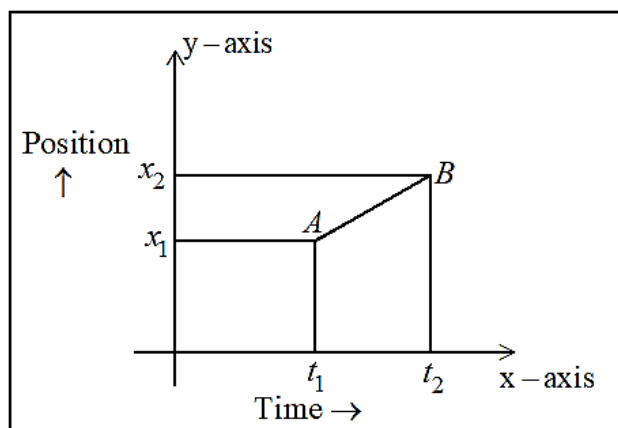
1. Slope of the tangent at any point gives instantaneous velocity.

$$\text{Slope } m = \tan \theta = \frac{PA}{OA}$$

$$= \frac{x}{t}$$

= velocity

2. The slope of the chord b/w two points gives average velocity.



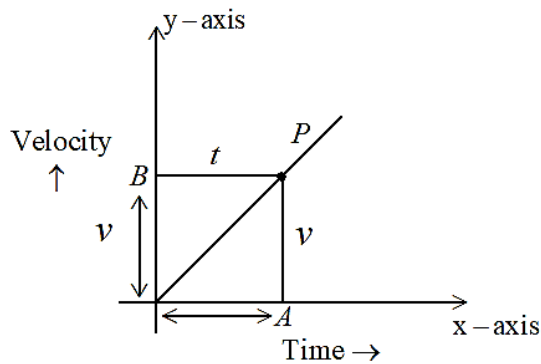
$$\text{Slope } (m) = \frac{y_2 - y_1}{x_2 - x_1} = \frac{x_2 - x_1}{t_2 - t_1}$$

= average velocity

Velocity time graphs [v-t graph]

Graphs are drawn with time along x axis and velocity along y axis.

1. Slope of the tangent at any point gives instantaneous acceleration.

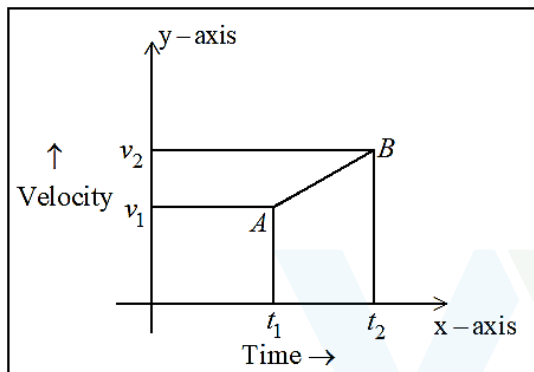


$$\text{Slope } m = \tan \theta = \frac{PA}{OA}$$

$$= \frac{v}{t}$$

= Instantaneous acceleration

2. The slope of the chord b/w two points gives average acceleration.

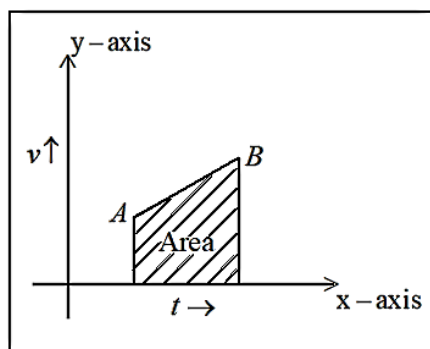


$$\text{Slope } (m) = \frac{y_2 - y_1}{x_2 - x_1} = \frac{v_2 - v_1}{t_2 - t_1}$$

= Average acceleration

3. The area under cover velocity-time graph gives displacement

Displacement (s) = Area of $v-t$ graph



Graphical method:-

Kinematical eqs. of motion of a body with uniform acceleration.

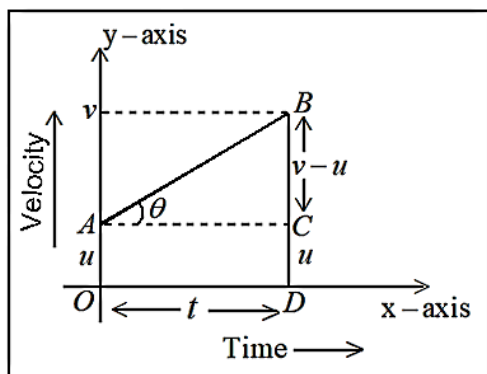
consider a particle moving with initial velocity u and uniform acceleration a .

Suppose v be the velocity after time t seconds

Let ' s ' be the displacement travelled in that time

The velocity time graph is a straight line with positive slope.

The graph is given by the line AB as shown in the figure.



To show that $v = u + at$:

Slope of the tangent from $v-t$ graph gives acceleration.

$$\tan \theta = \frac{BC}{AC} = \frac{v-u}{t} = a \Rightarrow at = v-u$$

$$\boxed{v = u + at}$$

To prove that $s = ut + \frac{1}{2}at^2$:

From the diagram

Displacement = Area under $v-t$ graph

$$s = \text{Area of rectangle } OACD + \text{Area of } \triangle ABC$$

$$s = (OD)(OA) + \frac{1}{2} AC \times BC$$

$$s = t(u) + \frac{1}{2} t(v-u)$$

$$s = ut + \frac{1}{2} t(at) \left[\because a = \frac{v-u}{t} \right]$$

$$s = ut + \frac{1}{2} at^2$$

If $s = x$ and $u = v_0$ then

$$x = v_0 t + \frac{1}{2} at^2$$

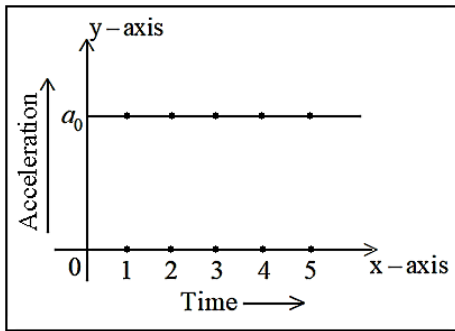
Acceleration-time graphs ($a-t$ graphs):

Graphs are drawn with time along x-axis and acceleration along y-axis.

Significances:

→ The slope of the tangent at any point gives Instantaneous Jerk.

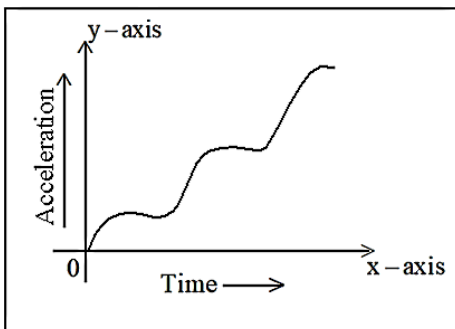
→ The area under covered $a-t$ graph gives changes in velocity ($v-u$)



→ Particle moves with constant acceleration (a_0)

→ The graph is a straight line parallel to x-axis

y-intercept = acceleration = a_0



Relative motion in one dimension:

Relative velocity: Velocity of one moving body with respect to other moving body is called relative velocity.

Let two objects A and B are moving uniformly with arrearage velocities v_A and v_B in one dimension says along x-axis having the positions $x_A(0)$ and $x_B(0)$ at $t = 0$ sec.

After $t = t$ sec

The position of A is $x_A(t) = x_A(0) + v_A t$

The position of B is $x_B(t) = x_B(0) + v_B t$

$$x_{BA}(t) = x_B(t) - x_A(t)$$

$$= x_B(0) - x_A(0) + (v_B - v_A)t$$

$$x_{BA}(t) = x_{BA}(0) + v_{BA}t$$

$$\therefore \vec{v}_{BA} = \vec{v}_B - \vec{v}_A$$

Similarly, $\vec{v}_{AB} = \vec{v}_A - \vec{v}_B$

$$\text{Avg velocity } v = \frac{x_2 - x_1}{t_2 - t_1}$$

$$v = \frac{x(t) - x(0)}{t - 0}$$

$$vt = x(t) - x(0)$$

$$x(t) = x(0) + vt$$

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